

Simplifying binomials

If we are asked to simplify the following binomials

$(5 + 2)(3 + 4)$ this is simple if we follow **PERMDAS** to help us simplify.

$(5 + 2)(3 + 4) = (7)(7) = 49$ using **PERMDAS**

However, there is a longer method used in algebra when we cannot simplify further in the parentheses. We will **use the distribution method and do the multiplication first.**

$(5 + 2)(3 + 4)$

- take the first term, **5**, in the first binomial
 - multiply it through each term in the second binomial
- take the second term, **2**, in the first binomial
 - multiply it through each term in the second binomial.

$$\begin{aligned}(5 + 2)(3 + 4) &= \overbrace{5(3 + 4)} + \overbrace{2(3 + 4)} \\ &= 15 + 20 + 6 + 8 \\ &= 49\end{aligned}$$

using the longer method, we still get the same answer

Let's look at why we need another method to help us simplify binomial expressions.

Simplify $(x + 3)(x + 7)$; We can see that we cannot simplify further inside the parentheses, so we must use the longer method to allow us to multiply binomials.

$$\begin{aligned}\text{Ex. } (x + 3)(x + 7) &= \overbrace{x(x + 7)} + \overbrace{3(x + 7)} \\ &= x^2 + 7x + 3x + 21 \\ &= x^2 + 10x + 21\end{aligned}$$

now add like terms

***notice how each and every term is distributed (multiplied) through.**

Simplify the following

$$\begin{aligned}\text{Ex. } (a + 5)(a - 3) &= \overbrace{a(a - 3)} + \overbrace{5(a - 3)} \\ &= a^2 - 3a + 5a - 15 \\ &= a^2 + 2a - 15\end{aligned}$$

add like terms

the simplified form

$$\begin{aligned}\text{Ex. } (x - 4)^2 &= (x - 4)(x - 4) \\ &= \overbrace{x(x - 4)} - \overbrace{4(x - 4)} \\ &= x^2 - 4x - 4x + 16 \\ &= x^2 - 8x + 16\end{aligned}$$

simplified form

Remember: pay attention to the signs of the terms as you are multiplying. This is where mistakes can happen. Take your time and understand the logic. **PERMDAS** guides you.